MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Match the given graph with its polynomial function.



SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

Describe the end behavior of the polynomial function by finding $\lim_{x \to \infty} f(x)$ and $\lim_{x \to \infty} f(x)$.

 $x \to \infty \qquad x \to -\infty$ 2) f(x) = -2x² + 2x³ + 6x - 5 3) f(x) = -3x⁴ - 5x² - 7

Find the zeros of the function.

4)
$$f(x) = x^3 - 16x$$

5) $f(x) = 3x^3 + 4x^2 + 1x$
6) $f(x) = x^2 + 9x + 20$

Describe the end behavior of the polynomial function by finding $\lim_{x \to \infty} f(x)$ and $\lim_{x \to \infty} f(x)$.

 $x \to \infty$ $x \to -\infty$ 7) f(x) = x³ + 2x² + 5x - 7

Find the zeros of the polynomial function and state the multiplicity of each.

8)
$$f(x) = -5x^2(x - 8)(x + 3)^3$$

9)
$$f(x) = 5(x + 7)^2(x - 7)^3$$



Find a cubic function with the given zeros. 12) 6, -4, 7

Divide f(x) by d(x), and write a summary statement in the form indicated.

13) $f(x) = 4x^3 - 14x^2 - 6x + 5; d(x) = 2x + 1$ (Write answer in polynomial form)

14)
$$f(x) = x^4 - 4x^3 - 2x^2 - 4x - 3; d(x) = x^2 + 1$$

(Write answer in fractional form)

Divide using synthetic division, and write a summary statement in fraction form.

15)
$$\frac{2x^3 + 3x^2 + 4x - 10}{x + 1}$$

Find the remainder when f(x) is divided by (x - k)16) f(x) = $2x^3 + 2x^2 + 3x + 4$; k= -2 17) f(x) = $x^5 + 4x^4 - 5x^3 + 2x^2 - 4x - 7$; k = 3

Use the Factor Theorem to determine whether the first polynomial is a factor of the second polynomial.

18) $x - 2; 5x^2 - 24x + 28$ 19) $x + 2; 6x^3 + 9x^2 - 5x + 2$

20)
$$x + 4$$
; $8x^4 + 33x^3 - 4x^2 + x + 4$

Use the graph to guess possible linear factors of f(x). Then completely factor f(x) with the aid of synthetic division.



Find the requested function.

22) Find the polynomial function with leading coefficient -7; degree 3; and -4, 4, and 2 as zeros.

Use the Rational Zeros Theorem to write a list of all potential rational zeros

23) $f(x) = 3x^3 + 37x^2 + 37x + 27$

24)
$$f(x) = 2x^3 + 5x^2 + 12x - 8$$

Find all rational zeros.

25) $f(x) = x^3 + 4x^2 - 27x - 90$

26)
$$f(x) = 10x^3 + 53x^2 + 14x - 5$$